

Temperature dissemination in a post-redefinition world

Dr. Patrick Rourke, National Research Council Canada

29th Meeting of the CCT – Session 2

4 November 2020

Review

The revision of the SI—the result of three decades of progress in metrology

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**THE KELVIN IS
DEAD,
LONG LIVE THE
KELVIN!**

The redefinition of the kelvin – what's next?

The CCT Declaration of 2014 acknowledges the known short-comings of both defined temperature scales (CCT 2014)

- For the ITS-90: 'inherent weaknesses, including known discrepancies from T '.
- For the PLTS-2000: 'currently no resolution of its inherent discrepancy of ~6 % at the lowest temperatures'.

and concludes that new thermodynamic temperature determinations are required to support:

- 'In the short term: the introduction and implementation of the *mise en pratique* ✓ the definition of the kelvin (MeP_K) through determining robust, reliable values of $T-T_{90}$ and $T-T_{2000}$ '. **Consensus**
- 'In the medium term: facilitate direct dissemination of the redefined kelvin through developing robust and reliable methodologies to disseminate T , particularly at the extremes of temperature $>1300\text{ K}$ and $<1\text{ K}$ '.
- 'In the long term: generate the background data required for a new unified temperature scale of improved thermodynamic consistency compared to the currently defined scales'.



Primary thermometers

- T : Thermodynamic temperature

Defined scales T_{scale} (approximations to T)

- T_{90} : International Temperature Scale of 1990 (ITS-90)
- T_{2000} : Provisional Low Temperature Scale of 2000 (PLTS-2000)
- T_{XX} : Future temperature scale (ITS-XX)

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SI Brochure – 9th edition (2019) – Appendix 2

20 May 2019

In the future, as the primary methods evolve and are expected to achieve lower uncertainties, primary thermometers will become more widely used and gradually replace the ITS-90 and the PLTS-2000 as the basis of temperature measurement.

- $< 1\text{ K} \rightarrow \text{middle} \leftarrow > 1300\text{ K}$
- Global transition likely messy and incomplete, smeared out in:
 - Time
 - Space
 - Temperature range
 - Position in calibration chain
- **Mixed dissemination environment**

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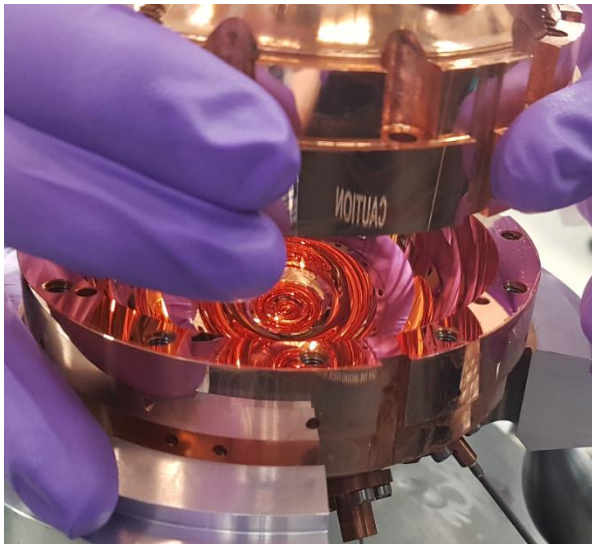
- 'In the long term: generate the background data required for a new unified temperature scale of improved thermodynamic consistency compared to the currently defined scales'.



Scale attributes (separable!):

- **Reproducibility**
- **Thermodynamic Accuracy**

Temperature dissemination in a post-redefinition world



OUTLINE

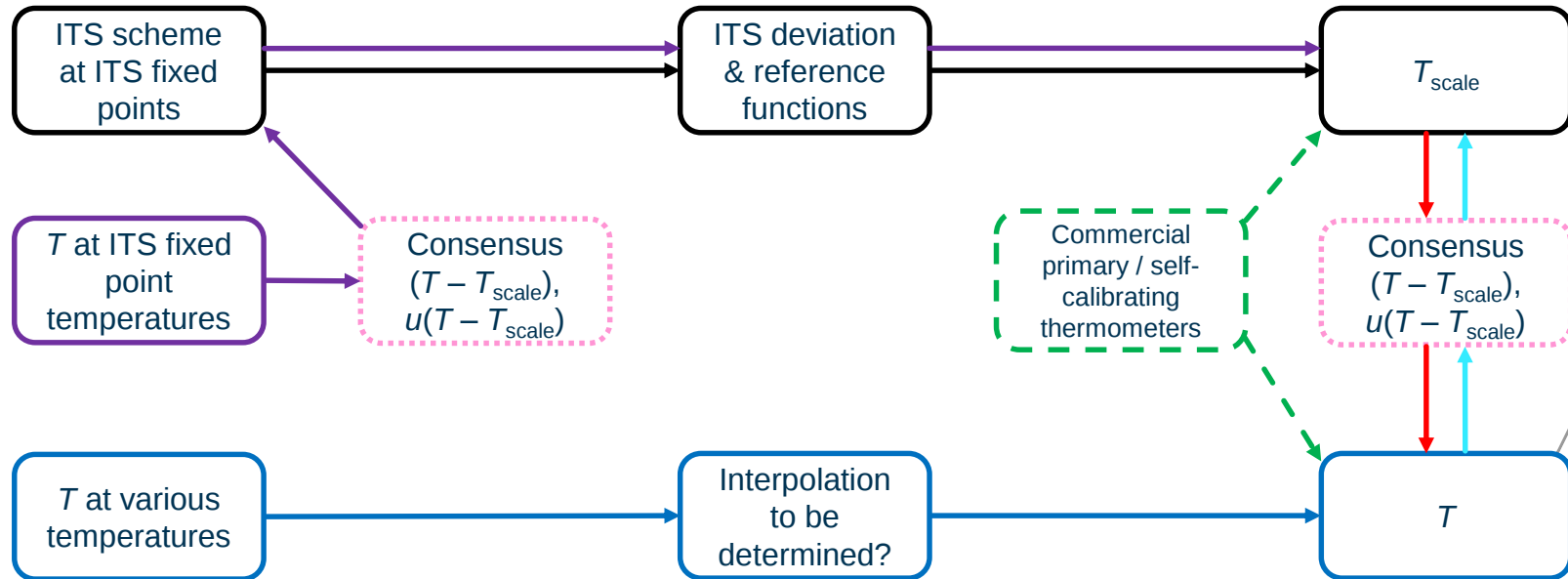
- Routes to dissemination
- Reproducibility: T_{90} vs. T_{xx} vs. T
- Dissemination path examples
- Thermodynamic inaccuracy of the ITS-90
- KCs and CMCs for primary thermometers
- Further T dissemination issues
- Summary and discussion

Routes to dissemination

CALIBRATION

INTERPOLATION & CONVERSION

REALIZATION



Reproducibility: T_{90} vs. T_{XX} vs. T

ILLUSTRATIVE EXAMPLE

- Capsule standard platinum resistance thermometer (CSPRT) calibration: T_{90} , T_{XX} , T
- Triple point of equilibrium hydrogen at 13.8033 K to triple point of water at 273.16 K
- NRC CSPRT comparison block data set, direct calculations from experimental measurements:
 - Type 1 non-uniqueness (subrange inconsistency “SRI”)
 - Type 3 non-uniqueness (artifact dependence “NU3”)
 - Propagation of uncertainties from fixed points (“PoU”)



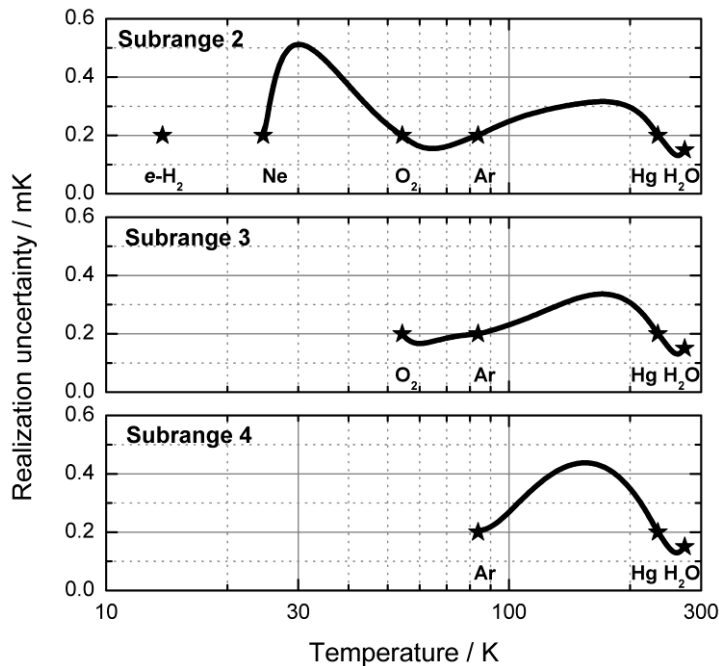
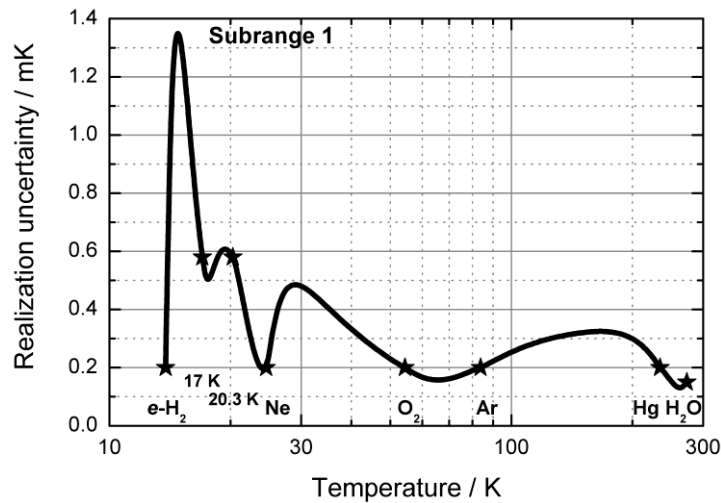
ITS-90 reproducibility, xenon fixed point substitution and new interpolating equations between 13.8033 K and 273.16 K

(To be submitted)

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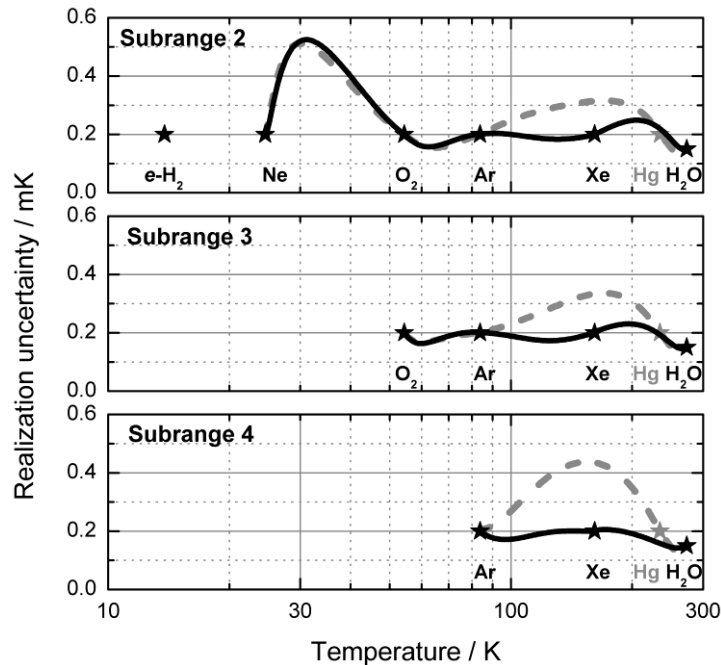
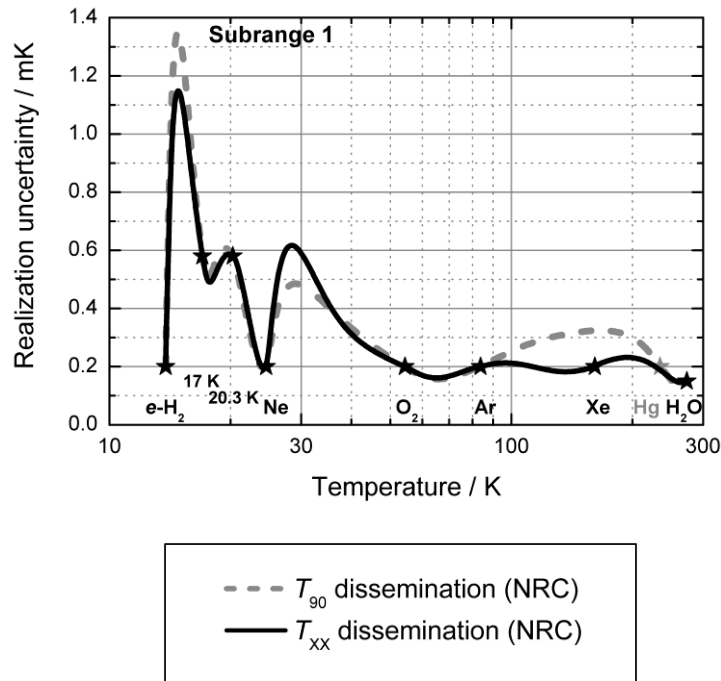
Reproducibility: T_{90}



NRC $k = 1$ CSPRT calibration uncertainties

- 0.15 mK @ TPW
- 0.20 mK @ Hg, Ar, O₂, Ne & e-H₂
- 0.58 mK @ 20.3 K & 17 K
- Hill *et al.* "CCT-K2.5 Final Report" 2015

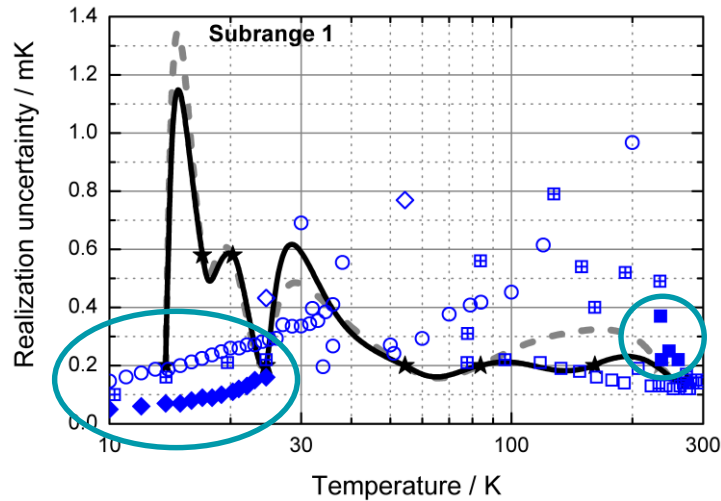
Reproducibility: T_{90} vs. T_{XX}



ITS-XX “Lite”

- Xenon replaces mercury
- New deviation functions for subranges 1, 2 & 3
- Same reference function as ITS-90
- More reproducible scale, same thermodynamic inaccuracy
- Minimally disruptive?

Reproducibility: T_{90} vs. T_{xx} vs. T

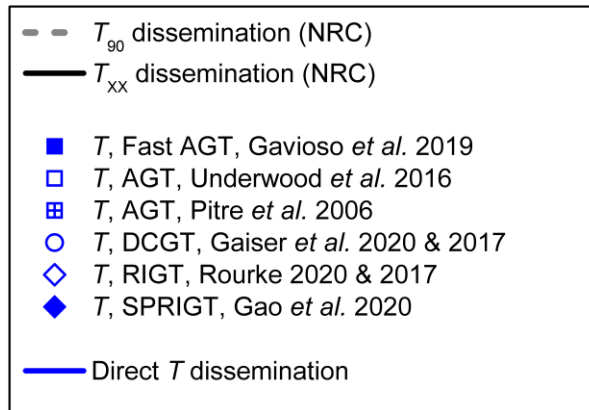
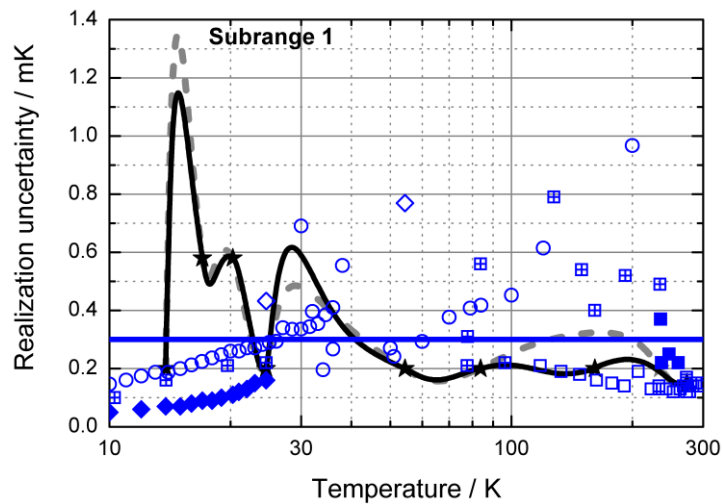


- T_{90} dissemination (NRC)
- T_{xx} dissemination (NRC)
- T , Fast AGT, Gavioso *et al.* 2019
- T , AGT, Underwood *et al.* 2016
- ▣ T , AGT, Pitre *et al.* 2006
- T , DCGT, Gaiser *et al.* 2020 & 2017
- ◇ T , RIGT, Rourke 2020 & 2017
- ◆ T , SPRIGT, Gao *et al.* 2020

$u(T)$

- Multiple techniques
- “Fast” methods
- Consistent low-temperature performance

Dissemination path examples: direct T dissemination



Direct T dissemination

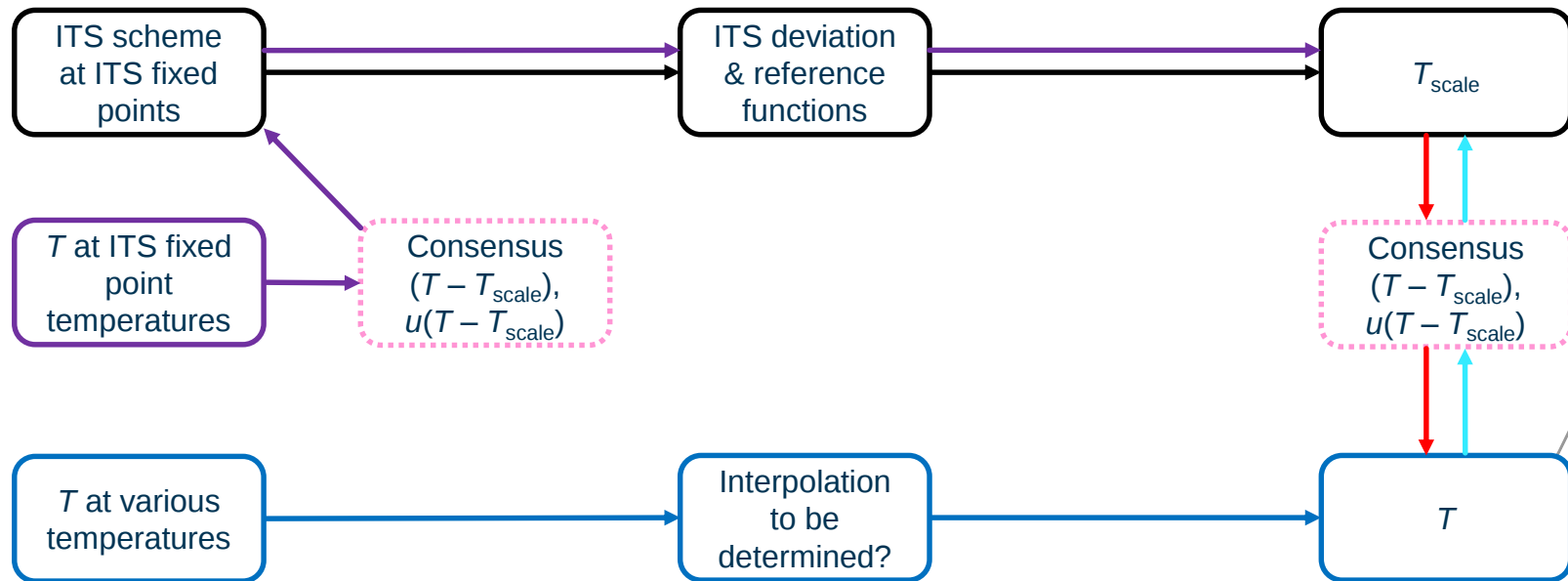
- Research vs. calibration
- $u(T) \sim 0.3$ mK likely attainable for dissemination with near-future technology

Dissemination path examples

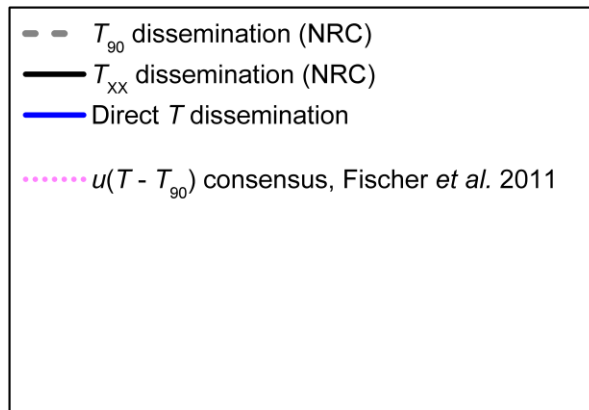
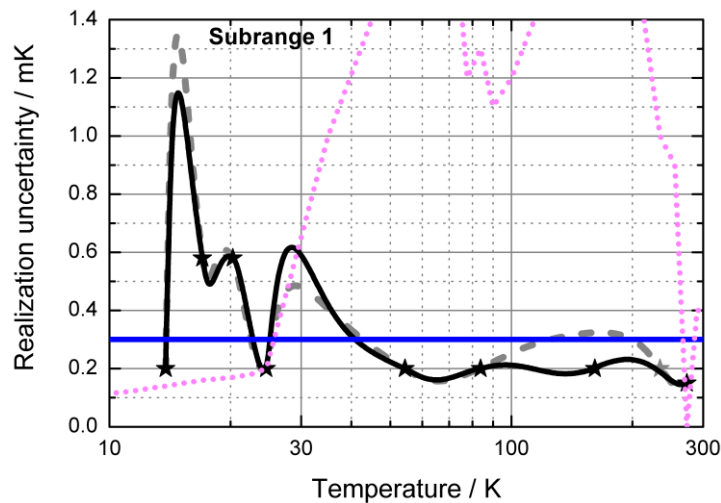
CALIBRATION

INTERPOLATION & CONVERSION

REALIZATION



Dissemination path examples: conversion using $(T - T_{\text{scale}})$ & $u(T - T_{\text{scale}})$



Community consensus 2011

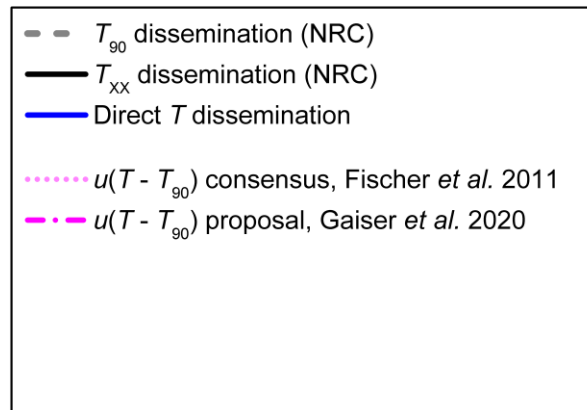
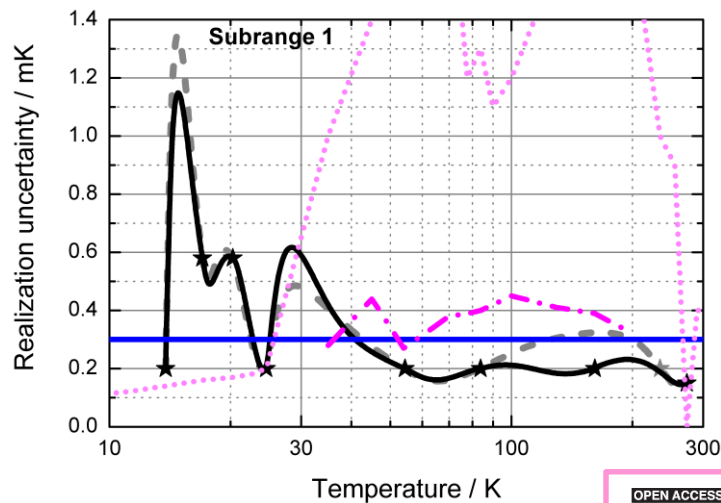
- $(T - T_{90})$
- $u(T - T_{90})$

Int J Thermophys (2011) 32:12–25
DOI 10.1007/s10765-011-0922-1

Present Estimates of the Differences Between Thermodynamic Temperatures and the ITS-90

J. Fischer · M. de Podesta · K. D. Hill ·
M. Moldover · L. Pitre · R. Rusby ·
P. Steur · O. Tamura · R. White · L. Wolber

Dissemination path examples: conversion using $(T - T_{\text{scale}})$ & $u(T - T_{\text{scale}})$



Community consensus

- Experimental work on-going worldwide, over entire temperature range of defined scales
- More reliable consensus $(T - T_{90})$ imminent?
- Gaiser *et al.* 2020
- CCT-WG-CTh
- 4 K to 303 K or 430 K?

OPEN ACCESS
IOP Publishing

Metrologia 57 (2020) 055003 (13pp)

Metrologia

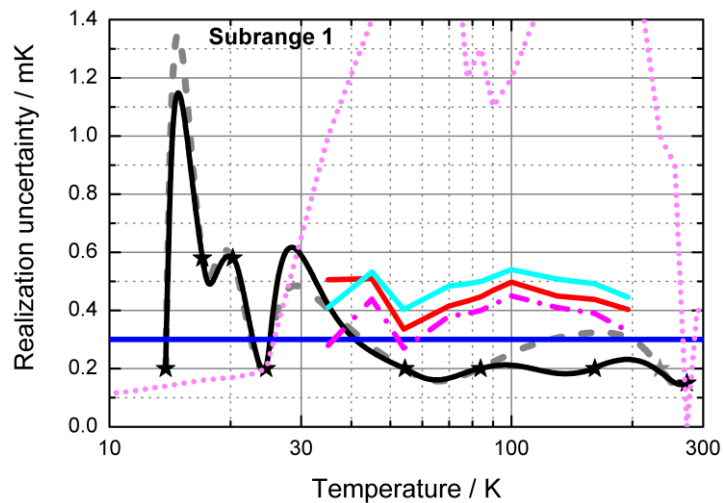
<https://doi.org/10.1088/1681-7575/ab9683>

Thermodynamic-temperature data from 30 K to 200 K

Christof Gaiser , Bernd Fellmuth and Norbert Haft

Physikalisch-Technische Bundesanstalt (PTB), Abbestrasse 2-12, 10587 Berlin, Germany

Dissemination path examples: conversion using $(T - T_{\text{scale}})$ & $u(T - T_{\text{scale}})$

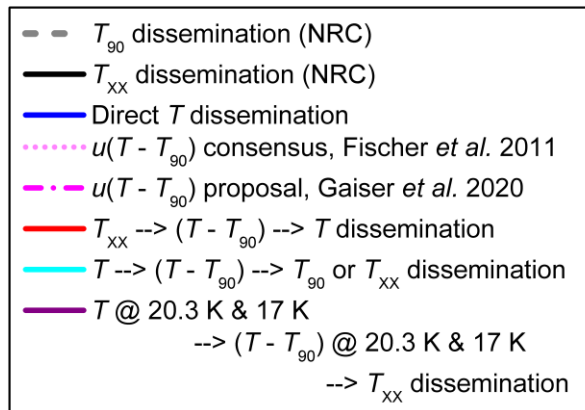
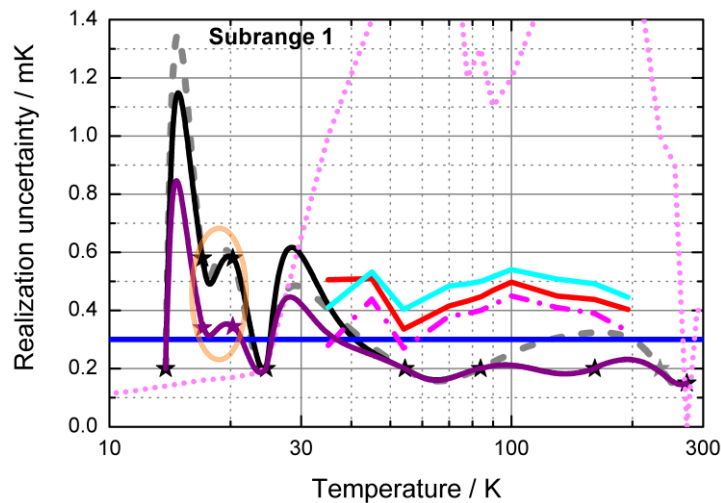


- T_{90} dissemination (NRC)
- T_{xx} dissemination (NRC)
- Direct T dissemination
- $u(T - T_{90})$ consensus, Fischer *et al.* 2011
- · - $u(T - T_{90})$ proposal, Gaiser *et al.* 2020
- $T_{xx} \rightarrow (T - T_{90}) \rightarrow T$ dissemination
- $T \rightarrow (T - T_{90}) \rightarrow T_{90}$ or T_{xx} dissemination

$T_{\text{scale}} \rightarrow T$

$T \rightarrow T_{\text{scale}}$

Dissemination path examples: T punch in at defined scale fixed point(s)

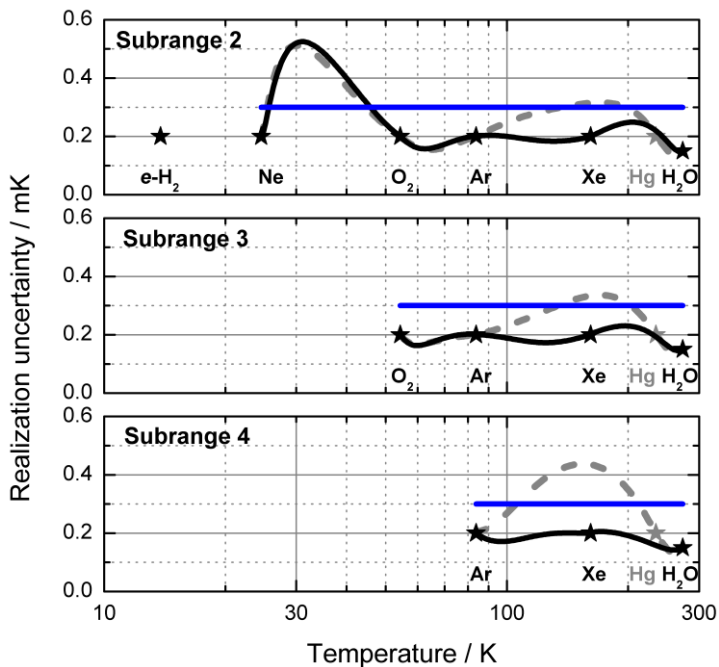
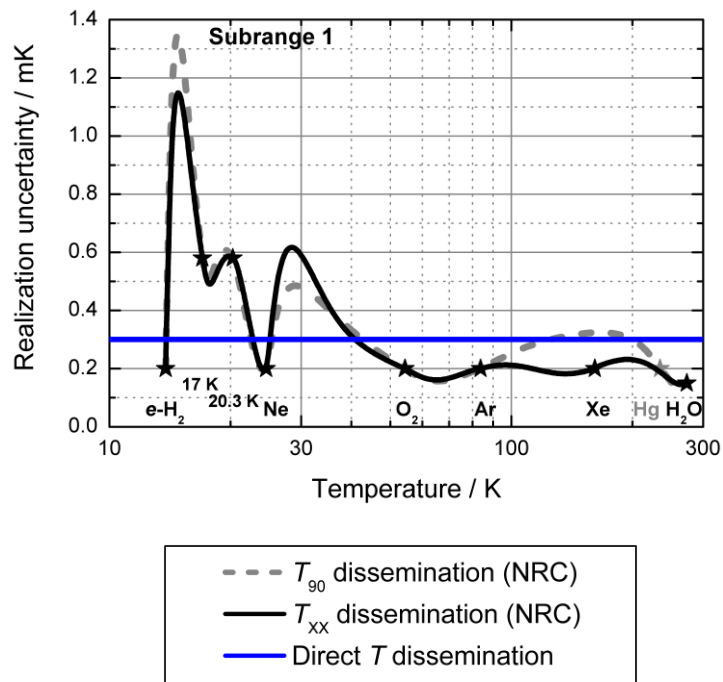


$T_{scale} \rightarrow T$

$T \rightarrow T_{scale}$

- Primary thermometers may replace:
 - Interpolating gas thermometers (IGTs)
 - Hydrogen vapour pressure (e-H₂ VP) systems
 - Other fixed points?

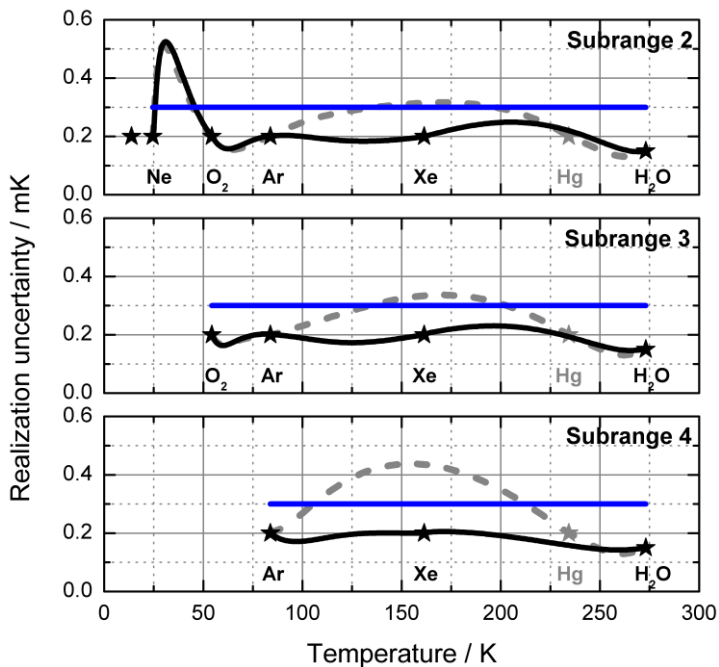
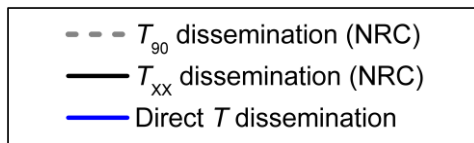
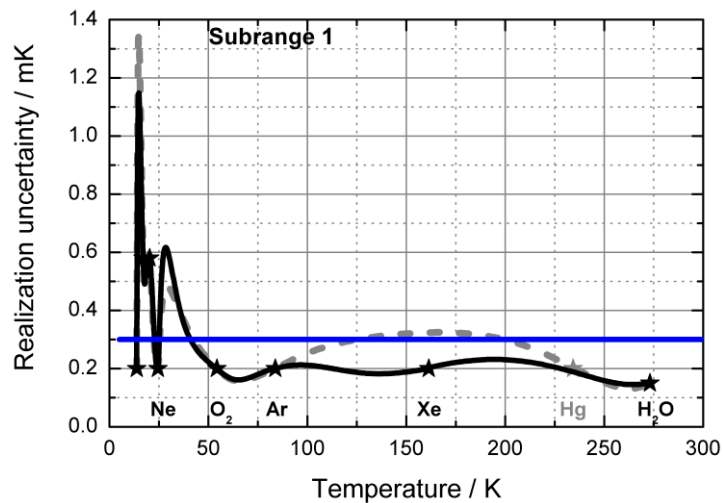
Dissemination path examples



Reproducibility of direct T competitive with defined scale

- Up to 24.5 K
- IGTs / e-H₂ VP systems already cumbersome
- Looks good in 24.5 K to 54 K range too

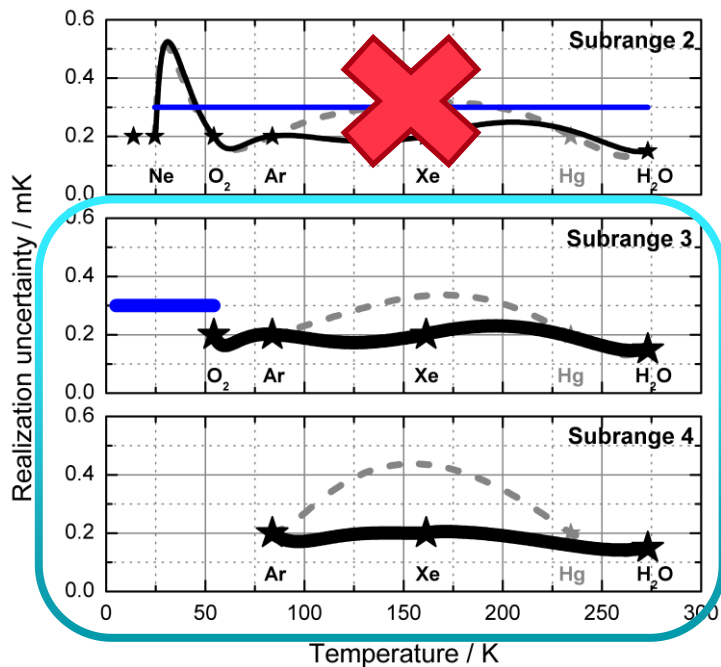
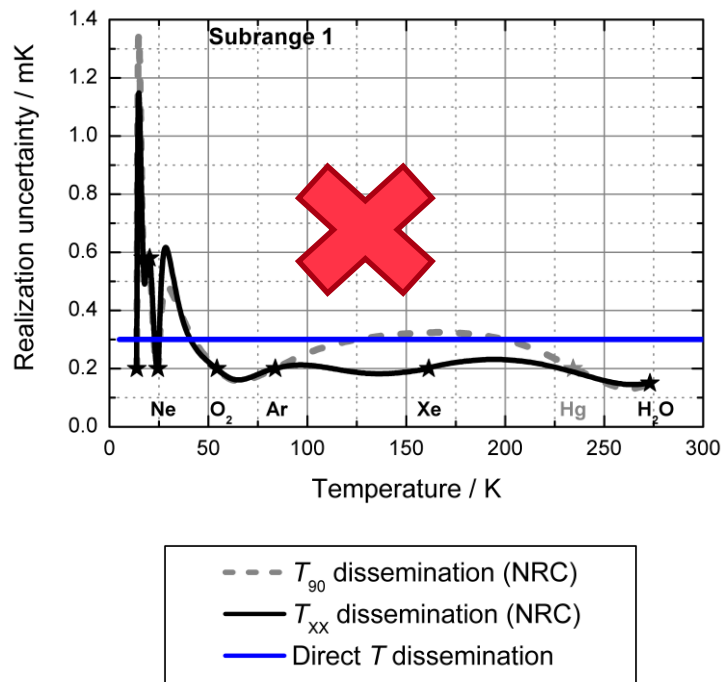
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Optimum reproducibility approach

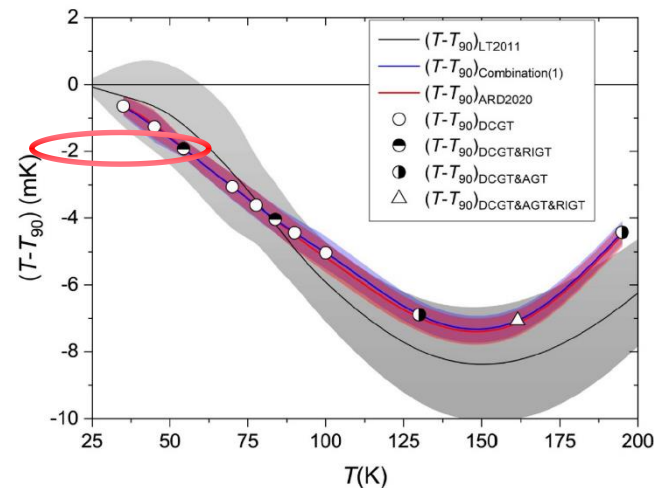


Dissemination:
 $T < 54 \text{ K}$, $T_{xx} > 54 \text{ K}$

- Primary thermometry displaces ITS subranges 1 & 2
- ITS-XX “Lite” subranges 3 & 4 have excellent reproducibility, need few calibration points
- Changeover at the triple point of oxygen

• But...

Thermodynamic inaccuracy of the ITS-90



ITS-90 is a poor approximation to thermodynamic temperature

- 2 mK discrepancy at 54 K = $10 \times u_{NRC}(T_{90})$
- Big step change if dissemination switches from T to approximation-to- T (defined scale) here
- Cross-converting incurs additional uncertainty
- Even worse at 84 K and beyond
- Problem may become pervasive, unless:
 - Direct dissemination of the kelvin according to its new definition is confined to temperature regions where $T_{scale} \approx T$; or
 - Thermodynamic accuracy of defined scales are improved

OPEN ACCESS

TOP Publishing

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Metrologia

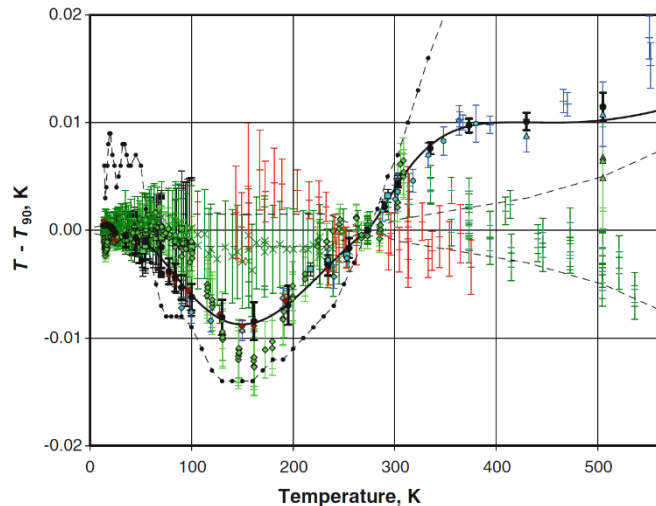
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At higher temperatures too

- $(T - T_{90}) \approx 400 \text{ mK} = 0.4 \text{ K}$ at 3000°C
- Second radiation constant $c_{2,90} \neq c_2 \equiv h c / k$
- Non-uniqueness of the ITS-90 $\approx 100 \text{ mK} = 0.1 \text{ K}$ at 3000°C

All are now defined constants of the SI

IOP Publishing

Metrologia 57 (2020) 045007 (7pp)

Metrologia

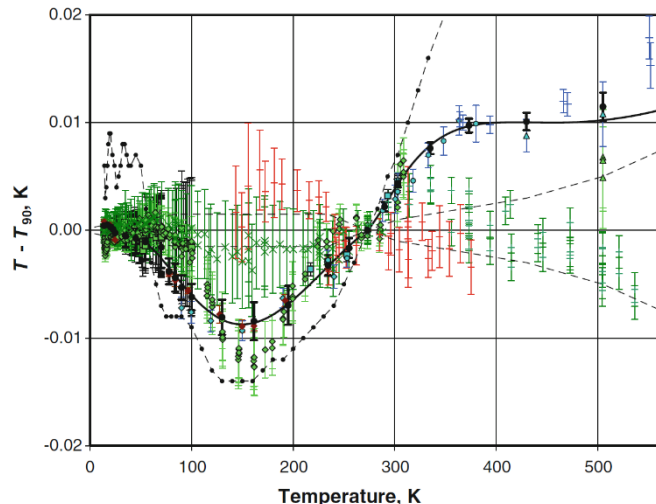
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The non-uniqueness of ITS-90 above the silver point and its impact on values of $T - T_{90}$

Peter Saunders

Measurement Standards Laboratory of New Zealand, PO Box 31-310, Lower Hutt, New Zealand

Thermodynamic inaccuracy of the ITS-90



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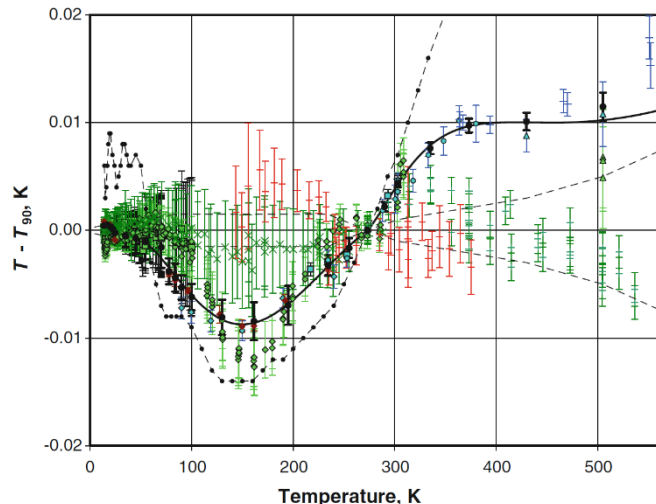
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- Dissemination patchwork:
 - Time
 - Space
 - Temperature range
 - Position in calibration chain
- Mixed dissemination environment
- **Danger of confusion between T and T_{90} in broader downstream community**

Thermodynamic inaccuracy of the ITS-90



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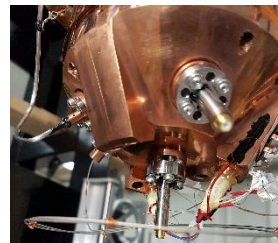
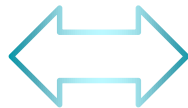
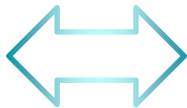
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- Dissemination patchwork:
 - Time
 - Space
 - Temperature range
 - Position in calibration chain
- Mixed dissemination environment
- **Danger of confusion between T and T_{90} in broader downstream community**
- Cost of confusion vs. cost of new scale?
- Metrology $\Rightarrow$ applications

ITS-XX “Deluxe”

KCs and CMCs for primary thermometers: beware pre-ITS-style laboratory scales!



Key Comparisons

- Exchanging primary thermometers unfeasible
- SPRTs as transfer standards?
 - What if reproducibility / stability of primary thermometers eclipses SPRTs?
 - *E.g.* improvement: lamps → radiation thermometers
- Additional uncertainty: $T \leftrightarrow T_{\text{scale}}$

Calibration and Measurement Capabilities

- Non-contact thermometry leading the way
 - Simultaneously handle CMC review process for T_{scale} & T
 - Higher uncertainties
 - Manageable NMI workload
- Commercial primary / “self-calibrating” thermometers?

Further T dissemination issues

To think about...

- Implications for core industrially-relevant long-stem SPRT range: triple point of argon (84 K) to freezing point of aluminum (660 °C)
- Calibration points, interpolation, non-uniqueness, propagation of uncertainty
 - Prescribed for defined scales; limited number of cal. points / subranges
 - Direct T dissemination cal. points & interpolation could be anything
 - More complicated if new interpolating instruments begin to be used at the highest levels (Task Group on Emerging Technologies!)
- What if primary thermometers not meeting criteria for inclusion in the *MeP-K* begin to be used “in the wild”?



LSPRTs on the way to NIST for CCT-K9

Summary and discussion



**The redefinition
of the kelvin –
what's next?**

Mixed T_{scale} and T dissemination world

- ITS-XX “Lite” more reproducible than ITS-90, same thermodynamic inaccuracy, low disruption
- Near future T dissemination: reproducibility likely competitive with defined scales up to 54 K
- Costs of downstream T & T_{scale} confusion vs. disruption of introducing thermodynamically-accurate ITS-XX “Deluxe”
- Better metrology enables new applications & technologies
- Primary thermometers:
 - Key Comparisons & Calibration and Measurement Capabilities
 - Implications for industrially-relevant 84 K to 660 °C LSPRT range
 - Calibration points, interpolation, non-uniqueness, propagation of uncertainty



THANK YOU

Patrick Rourke • patrick.rourke@nrc-cnrc.gc.ca